Name the Six

We have a set of 6 positive integers about which we have calculated the following: $maximum = 24, \quad mean = 10, \quad median = 5, \quad and the mode is one (1).$ List the six numbers.

Bonus: Construct a similar problem which gives statistical measures on a unique, solvable set of integers, and describe a solution method for it.

Solutions

The six are 1, 1, 1, 9, 24 and 24.

The required members at the outset are 1, 1, a, b, c and 24. Since the median is 5, a+b = 10. The sum of the set is 60 which requires c = 24. Since the mode is one (1), there must be a third occurrence of it. Setting a = 1, gives b = 9.